

カードベース暗号と論理パズル

岩本貢@電気通信大学大学院情報理工学研究科

離散数学講義資料

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カードベース暗号プロトコル [B. den Boer, 1989]

↑ 使うカード: 2種類: ♣





◈ 符号化:

$$\bullet$$
 0 \mapsto 0 1 \mapsto 1





暗号化 (隠す)





* 背後での操作(背面操作): OK

カードベース暗号プロトコル [B. den Boer, 1989]

- * 使うカード: 2種類:

- * 符号化:
 - * $0 \mapsto \boxed{0}$ $1 \mapsto \boxed{1}$
- * 暗号化 (隠す)
 - * 裏返す: 1 + 1
 - * 背後での操作(背面操作):OK

今日の話題:金持ち比べ







- * A. C-C Yao (1982)
- ◆ 二人の金持ちがどちらがリッチか知りたい
 - * どちらも自分の資産を(大小以外)教えたくない
- * 技術的には、二者間秘匿計算問題、という

$$a=(a_n\cdots a_1)_2$$
 と $b=(b_n\cdots b_1)_2$ を最下位から比較

単にボブにビットを送る

$$a = (0 \ 0 \ 0)_2$$





$$b = (0 \ 1 \ 0)_2$$



$$a=(a_n\cdots a_1)_2$$
 と $b=(b_n\cdots b_1)_2$ を最下位から比較

単にボブにビットを送る

$$a = (0 \ 0 \ 0)_2$$





$$b = (0 \ 1 \ 0)_2$$



 $a_i \neq b_i$ ならば "Record"を b_i で置き換え

1st bit 2nd bit 3rd bit
Record R

$$a=(a_n\cdots a_1)_2$$
 と $b=(b_n\cdots b_1)_2$ を最下位から比較

単にボブにビットを送る

$$a = (0 \ 0 \ 0)_2$$



$$egin{aligned} a_i \in \{ egin{aligned} oldsymbol{0} & oldsymbol{1} \ \end{pmatrix} \end{aligned}$$

$$b = (0 \ 1 \ 0)_2$$



 $a_i \neq b_i$ ならば "Record"を b_i で置き換え

1st bit 2nd bit 3rd bit Record R そのまま

$$a=(a_n\cdots a_1)_2$$
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$$egin{pmatrix} a_i \ \in \{ egin{bmatrix} oldsymbol{0} \ oldsymbol{1} \ \end{pmatrix}$$

$$b = (0 \ 1 \ 0)_2$$



 $a_i \neq b_i$ ならば "Record"を b_i で置き換え

1st bit 2nd bit 3rd bit Record R 1 2nd bit そのまま 置き換え

$$a=(a_n\cdots a_1)_2$$
 と $b=(b_n\cdots b_1)_2$ を最下位から比較

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$$a = (0 \ 0 \ 0)_2$$



$$egin{picture} oldsymbol{\dot{a}}_i \in \{oldsymbol{f 0} oldsymbol{f 1}\} \end{pmatrix}$$

$$b = (0 \ 1 \ 0)_2$$



 $a_i \neq b_i$ ならば "Record"を b_i で置き換え

1st bit 2nd bit 3rd bit
Record R 1

そのまま 置き換え そのまま

$$a=(a_n\cdots a_1)_2$$
 と $b=(b_n\cdots b_1)_2$ を最下位から比較



単にボブにビットを送る

$$a = (0 \ 0 \ 0)_2$$



$$egin{aligned} \dot{a}_i \end{pmatrix} \in \left\{ egin{bmatrix} oldsymbol{0} & oldsymbol{1} \end{matrix}
ight\} \end{aligned}$$

$$b = (0 \ 1 \ 0)_2$$



 $a_i \neq b_i$ ならば "Record"を b_i で置き換え

1st bit 2nd bit 3rd bit Record R 1 1 1 そのまま 置き換え そのまま

ダミーカード&アリスに嘘をつかせる

$$a = (0 \ 0 \ 0)_2$$





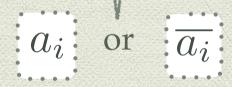


ダミーカード&アリスに嘘をつかせる



$$a = (0 \ 0 \ 0)_2$$





$$b = (0 \ 1 \ 0)_2$$

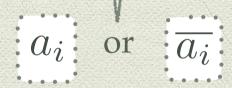


ダミーカード&アリスに嘘をつかせる



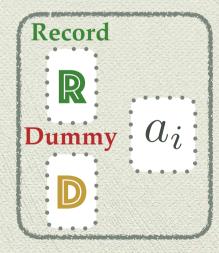
$$a = (0 \ 0 \ 0)_2$$











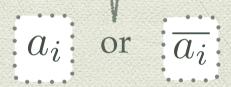
| | 1st bit | 2nd bit | 3rd bit |
|--------|---------|---------|---------|
| Record | R | | |
| Dummy | D | | |

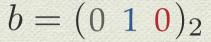
ダミーカード&アリスに嘘をつかせる



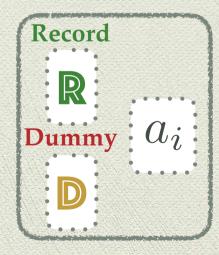
$$a = (0 \ 0 \ 0)_2$$











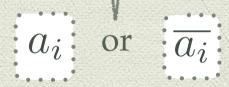
| | 1st bit | 2nd bit | 3rd bit |
|--------|---------|---------|---------|
| Record | R | | |
| Dummy | 0 | | |

ダミーカード&アリスに嘘をつかせる



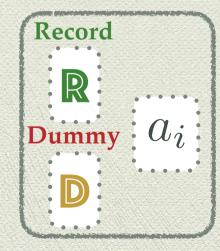
$$a = (0 \ 0 \ 0)_2$$





$$b = (0 \ 1 \ 0)_2$$





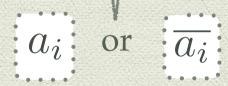
| | 1st bit | 2nd bit | 3rd bit |
|--------|---------|---------|---------|
| Record | R | 1 | |
| Dummy | 0 | | |

ダミーカード&アリスに嘘をつかせる



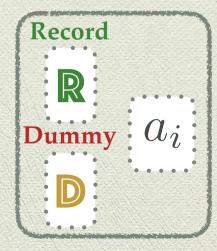
$$a = (0 \ 0 \ 0)_2$$





$$b = (0 \ 1 \ 0)_2$$





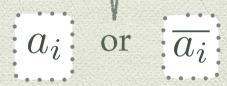
| | 1st bit | 2nd bit | 3rd bit |
|--------|---------|---------|---------|
| Record | R | 1 | |
| Dummy | D | | |

ダミーカード&アリスに嘘をつかせる



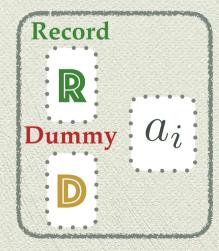
$$a = (0 \ 0 \ 0)_2$$





$$b = (0 \ 1 \ 0)_2$$





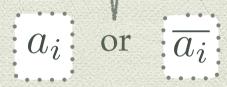
| | 1st bit | 2nd bit | 3rd bit |
|--------|---------|---------|---------|
| Record | R | 1 | |
| Dummy | D | 0 | 0 |

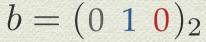
ダミーカード&アリスに嘘をつかせる



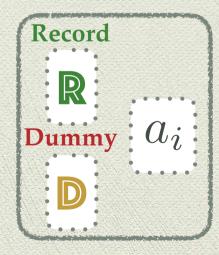
$$a = (0 \ 0 \ 0)_2$$











| | 1st bit | 2nd bit | 3rd bit |
|--------|---------|---------|---------|
| Record | R | | (1) |
| Dummy | D | | 0 |

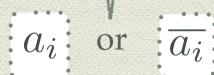
ダミーカード&アリスに嘘をつかせる



正直に振る舞うか嘘をつく

 $a = (0 \ 0 \ 0)_2$

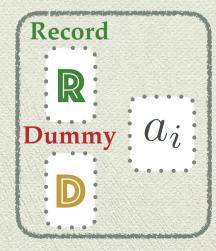




比べようがない!







| | 1st bit | 2nd bit | 3rd bit |
|--------|---------|---------------|---------|
| Record | R | | 1 |
| Dummy | D | O Paragraphia | 0 |

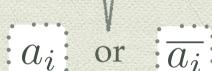
ダミーカード&アリスに嘘をつかせる



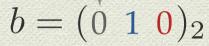
正直に振る舞うか嘘をつく

 $a = (0 \ 0 \ 0)_2$

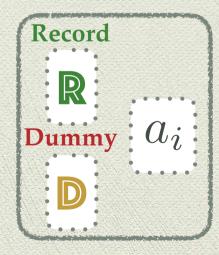






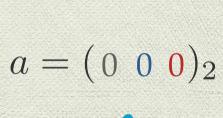




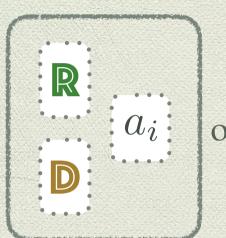


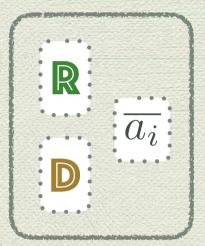
| | 1st bit | 2nd bit | 3rd bit |
|--------|--|---------|---------|
| Record | R | | 1 |
| Dummy | And former was a great of the state of the s | | 0 |
| + もう- | -工夫 | (次のス | ライド) |

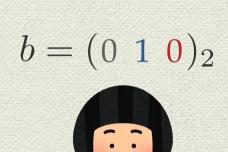
[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]



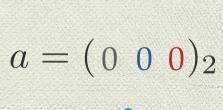




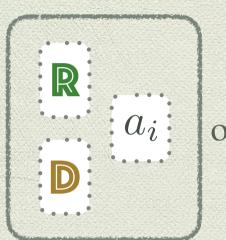


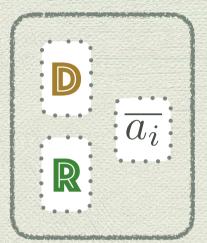


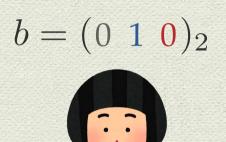
[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]









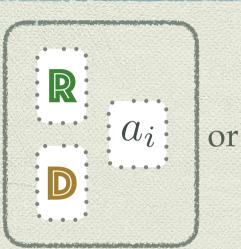


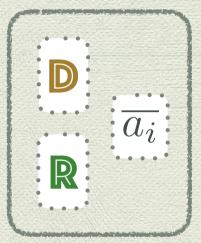
[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]

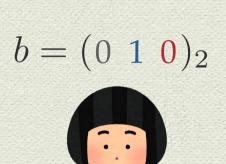
アリスはこれを 背面で準備

$$a = (0 \ 0 \ 0)_2$$







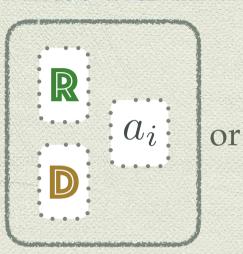


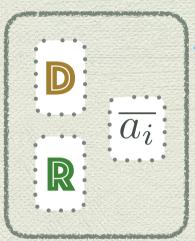
[Nakai-Misawa-Tokushige-lwamoto-Ohta, CANS2016]

アリスはこれを 背面で準備

$$a = (0 \ 0 \ 0)_2$$







どちらか知って いるのはアリスだけ

$$b = (0 \ 1 \ 0)_2$$

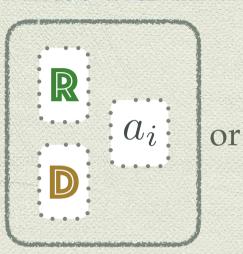


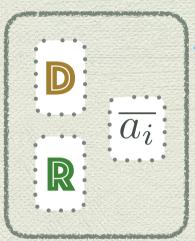
[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]

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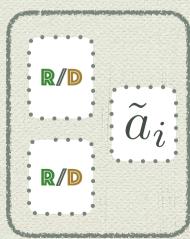




どちらか知って いるのはアリスだけ

$$b = (0 \ 1 \ 0)_2$$



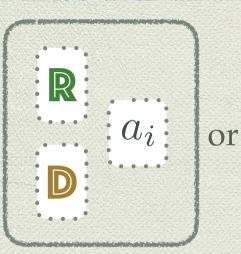


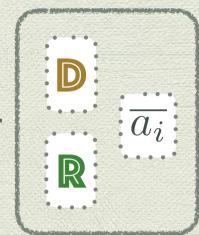
[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]

アリスはこれを 背面で準備

$$a = (0 \ 0 \ 0)_2$$





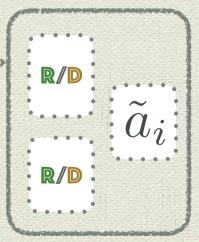


どちらか知って いるのはアリスだけ

$$b = (0 \ 1 \ 0)_2$$



Top $\tilde{a}_i \neq b_i$ b_i で置き換え

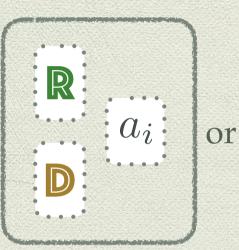


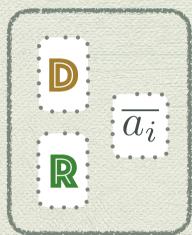
[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]

アリスはこれを 背面で準備

$$a = (0 \ 0 \ 0)_2$$







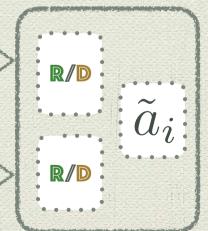
どちらか知って いるのはアリスだけ

$$b = (0 \ 1 \ 0)_2$$



Top $\tilde{a}_i \neq b_i$ b_i で置き換え

Bottom
$$\tilde{a}_i = b_i$$
 b_i で置き換え

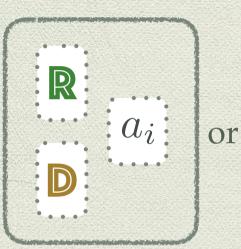


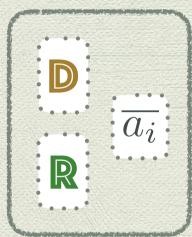
[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]

アリスはこれを 背面で準備

$$a = (0 \ 0 \ 0)_2$$







どちらか知って いるのはアリスだけ

$$b = (0 \ 1 \ 0)_2$$



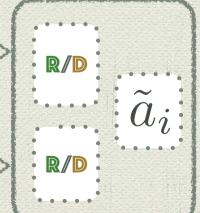
Top/Bottom strategy

ボブは背面で操作 どちらか知っている のはボブだけ Тор

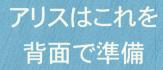
 $\tilde{a}_i \neq b_i$ b_i で置き換え

Bottom

 $\tilde{a}_i = b_i$ b_i で置き換え

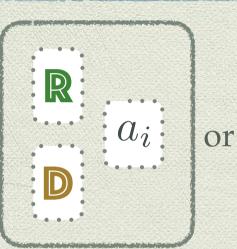


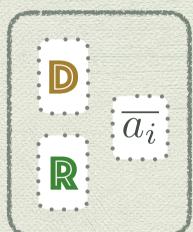
[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]



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どちらか知って いるのはアリスだけ

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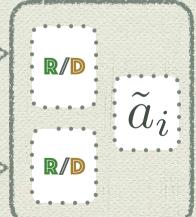
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ボブは背面で操作 どちらか知っている のはボブだけ Тор

 $\tilde{a}_i \neq b_i$ b_i で置き換え

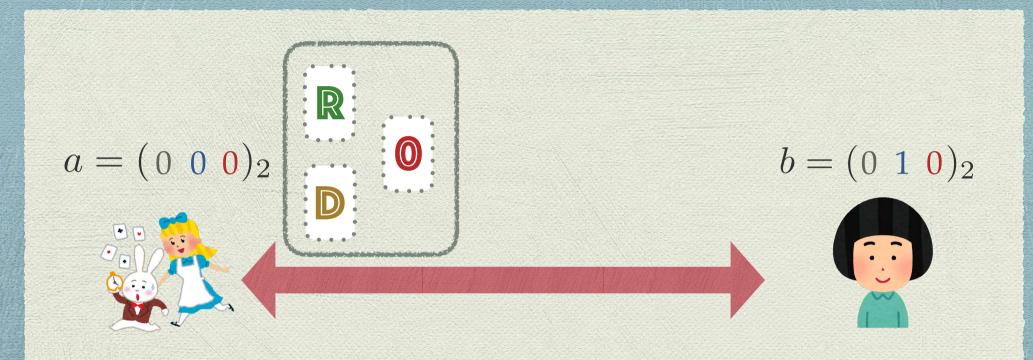
Bottom

 $\tilde{a}_i = b_i$ b_i で置き換え



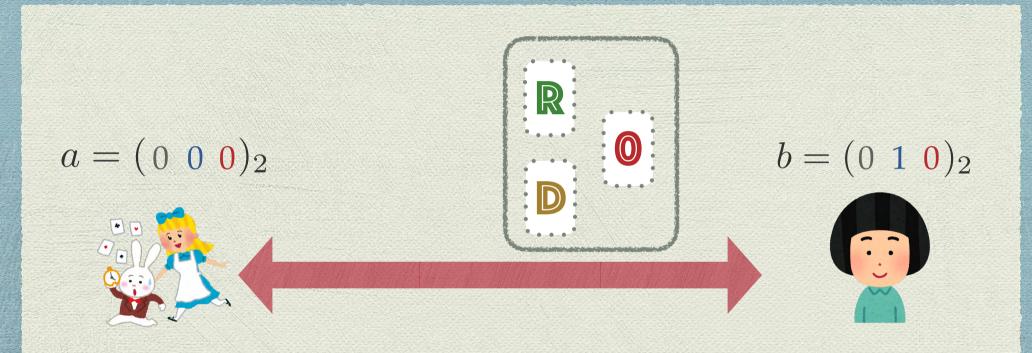
プロトコルの実行例:1st Round

[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]



プロトコルの実行例:1st Round

[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]

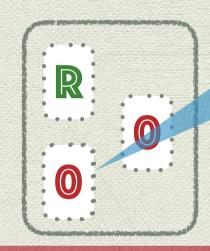


プロトコルの実行例:1st Round

[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]





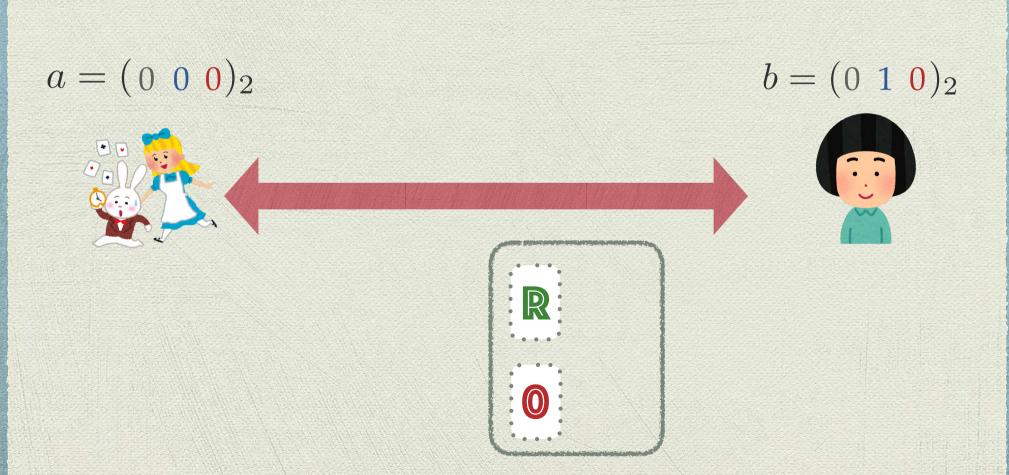


ボブは Bottom を 0 で置き換える

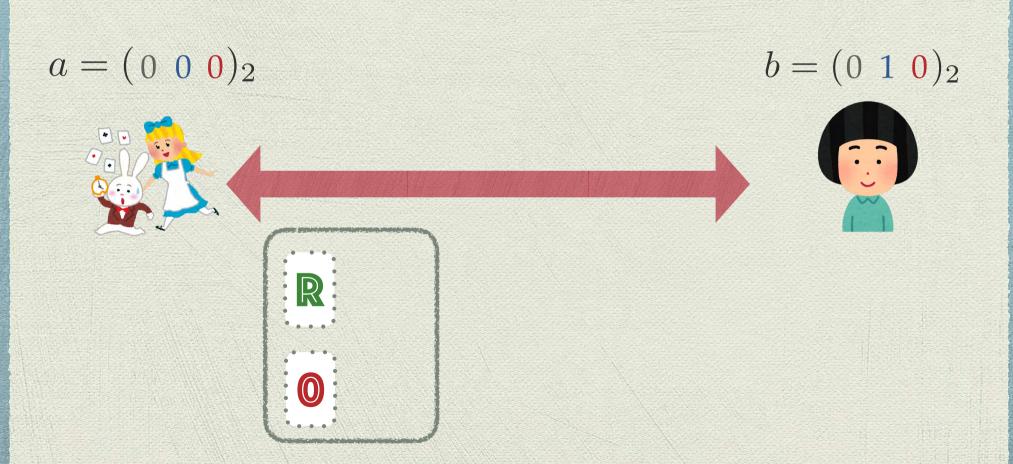
$$b = (0 \ 1 \ 0)_2$$



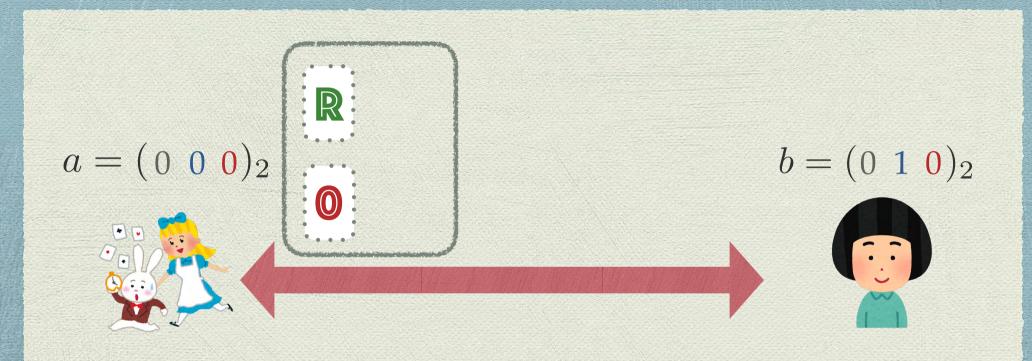
プロトコルの実行例:1st Round

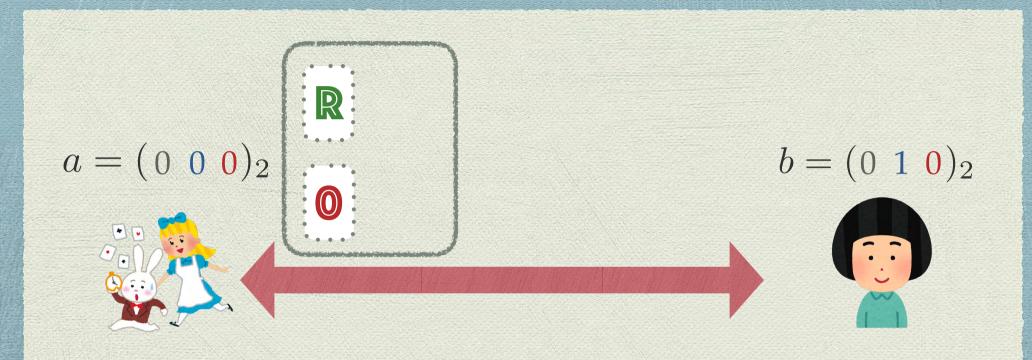


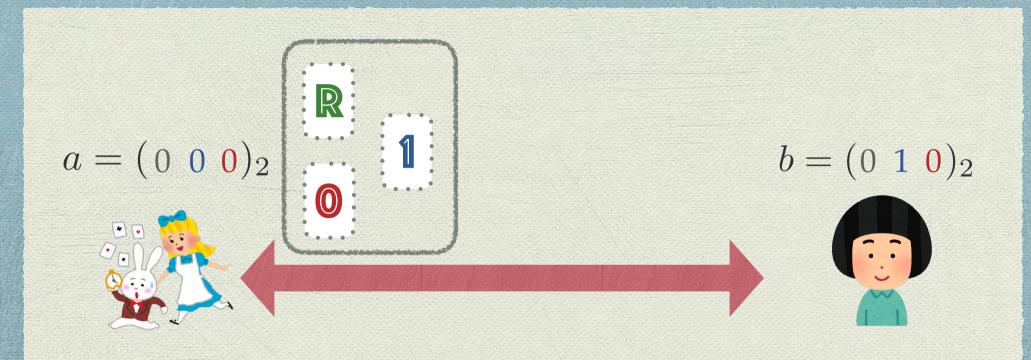
プロトコルの実行例:1st Round

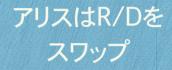


プロトコルの実行例:1st Round









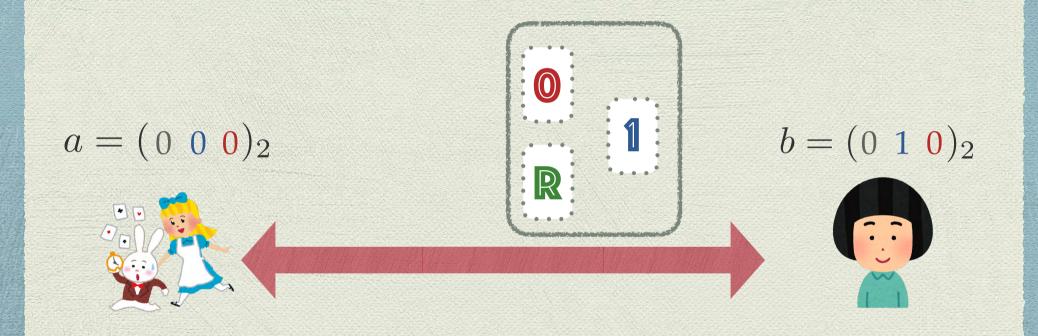
$$a = (0 \ 0 \ 0)_2$$



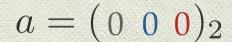


$$b = (0 \ 1 \ 0)_2$$

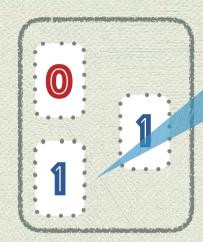




[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]



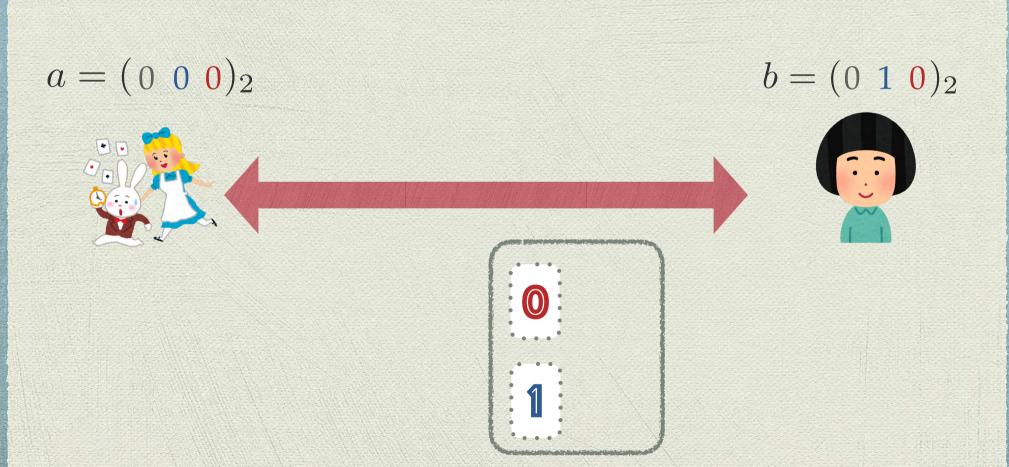


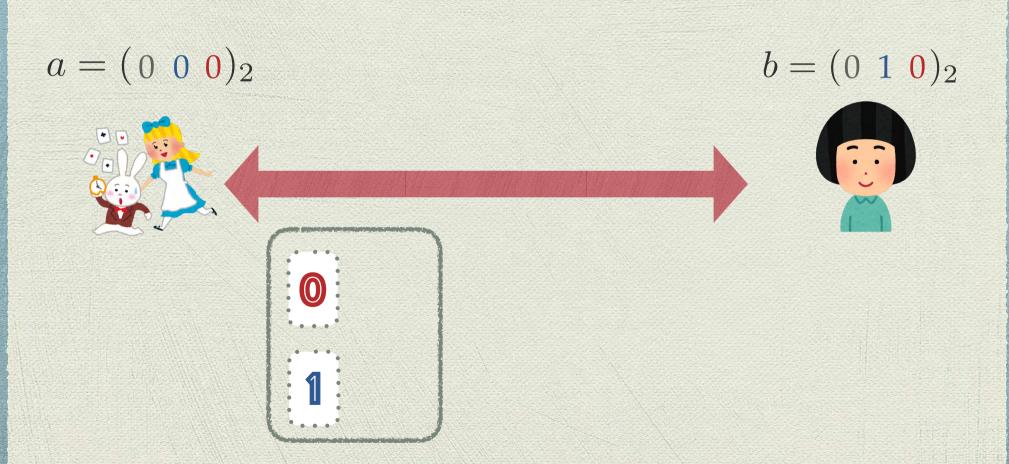


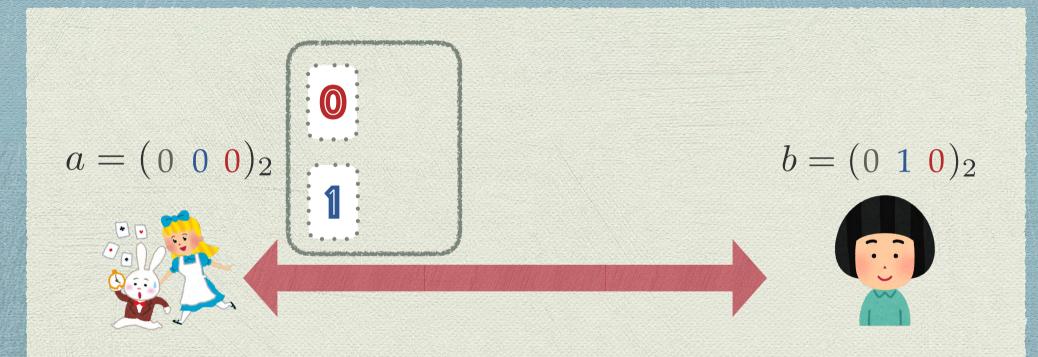
ボブは Bottom を 1 で置き換える

$$b = (0 \ 1 \ 0)_2$$

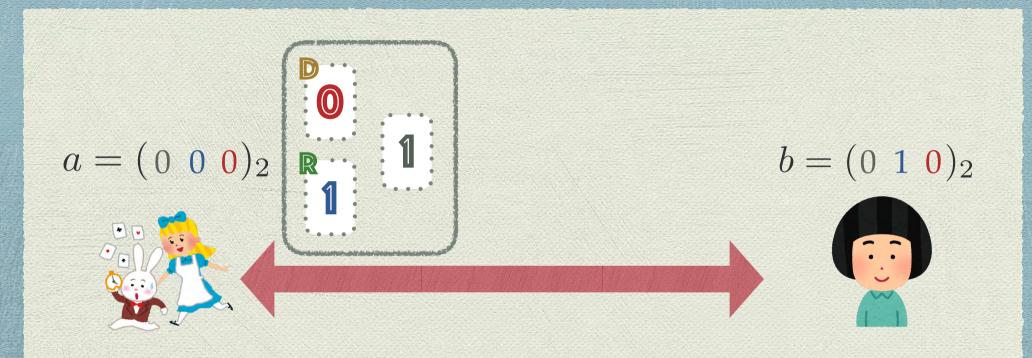


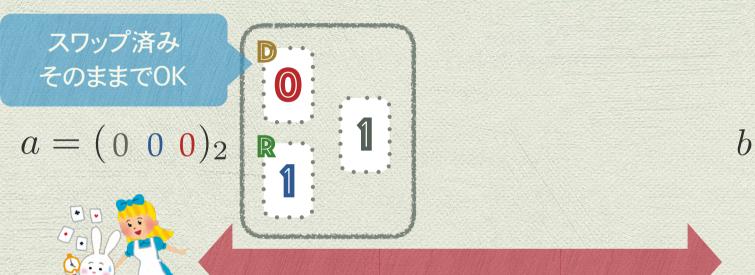


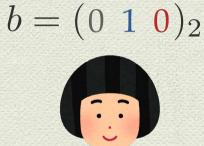


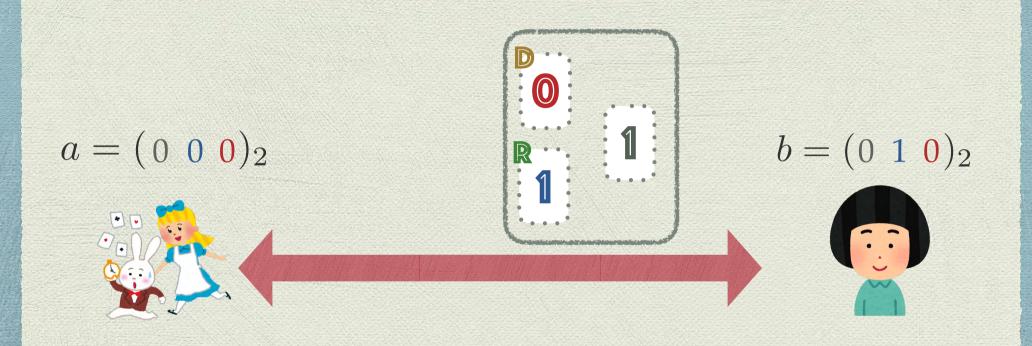




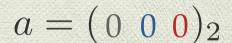




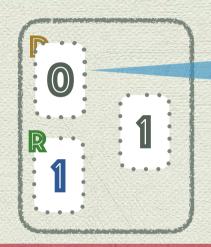




[Nakai-Misawa-Tokushige-Iwamoto-Ohta, CANS2016]



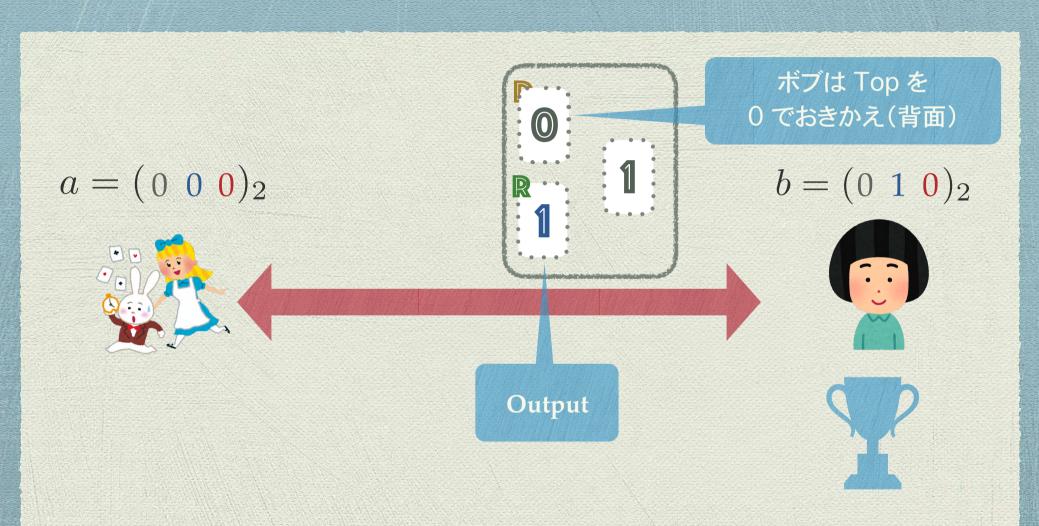




ボブは Top を 0 でおきかえ(背面)

$$b = (0 \ 1 \ 0)_2$$







この話 嘘つき島と同じだということに 気がつきましたか?

整理:

『嘘つき村問題』との関係



この道が「正直村」に行く場合:

[Q] この道はあなたの村に行きますか?

| | 正直村の住人か | He says |
|-------|---------|---------|
| 正直村の人 | True | Yes |
| 嘘つき村の | False | Yes |



 $a_i \neq b_i$ である場合

[Q] "Record" が置き換えられるか?

Top/Bottom strategy

| | $\tilde{a}_i \neq b_i$ | Record が置き換わる |
|----------------------|------------------------|-------------------|
| a_i を送る | True ($Top = Rec.$) | Yes (Top が置き換わる) |
| $\overline{a_i}$ を送る | False (Bot. = Rec.) | Yes (Bottom が換わる) |

まとめ

- * 『金持ち比べ問題』に対するカードベース暗号プロトコルの提案
- * 興味深い関係
 - * セキュリティ (マルチパーティ計算)
 - * 論理(『嘘つき村問題』)
- * 効率性ほか(省略)
 - * 先行研究より以下の指標で優れていることが分かっている
 - ◆ 使用するカード枚数
 - * 通信回数





おわり



